

Since, the quantity $\frac{1}{\rho} \frac{d\rho}{dt}$ is the same for all particles, it follows that the velocity of the particles is proportional to the distance from the center of mass.